Non-Poissonian Quantum Jumps of a Fluxonium Qubit due to Quasiparticle Excitations


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As the energy relaxation time of superconducting qubits steadily improves, nonequilibrium quasiparticle excitations above the superconducting gap emerge as an increasingly relevant limit for qubit coherence. We measure fluctuations in the number of quasiparticle excitations by continuously monitoring the spontaneous quantum jumps between the states of a fluxonium qubit, in conditions where relaxation is dominated by quasiparticle loss. Resolution on the scale of a single quasiparticle is obtained by performing quantum nondemolition projective measurements within a time interval much shorter than $T_1$, using a quantum-limited amplifier (Josephson parametric converter). The quantum jump statistics switches between the expected Poisson distribution and a non-Poissonian one, indicating large relative fluctuations in the quasiparticle population, on time scales varying from seconds to hours. This dynamics can be modified controllably by injecting quasiparticles or by seeding quasiparticle-trapping vortices by cooling down in a magnetic field.

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A mesoscopic superconducting circuit, of typical size smaller than 1 mm$^2$, cooled to a temperature well below the superconducting gap, should be completely free of thermal quasiparticle (QP) excitations. However, in the last decade, there has been growing experimental evidence that the QP density at low temperatures saturates to values orders of magnitude above the value expected at thermal equilibrium [1–5]. These nonequilibrium QP excitations limit the performance of a variety of superconducting devices, such as single-electron turnstiles [6], kinetic inductance [7,8], and quantum capacitance [9] detectors, microcoolers [10,11], as well as Andreev bound state nanosystems [12,13]. Moreover, QPs are an important intrinsic decoherence mechanism for superconducting two level systems (qubits) [14–19]. In particular, a recent experiment performed on the fluxonium qubit showed energy relaxation times in excess of 1 ms, limited by QPs [20]. Surprisingly, the sources generating these QP excitations are not yet positively identified. The measurement of nonequilibrium QP dynamics at low temperatures could provide insight into their origin as well as an efficient tool to quantify QP suppression solutions.

In this Letter, we show that the quantum jumps [21] of a qubit whose lifetime is limited by QP tunneling, such as the fluxonium artificial atom, can serve as a sensitive probe of QP dynamics. A jump in the state of the qubit indicates an interaction of the qubit with a QP, and therefore, fluctuations in the rate of quantum jumps are directly linked to changes in QP number. Tracking the state of the qubit in real time requires fast, single-shot projective measurement with minimal added noise, made possible by the advent of quantum-limited amplifiers [22–24]. In this work, we use a Josephson parametric converter (JPC) quantum-limited amplifier [23,25] to monitor the state of our qubit with a resolution of 5 μs, 2 orders of magnitude faster than the qubit lifetime. We find that the qubit jump statistics fluctuates between Poissonian and non-Poissonian, corresponding to a change in the QP number. Surprisingly, these fluctuations do not average over time scales ranging from seconds to hours. The quantum jumps we measure in this work are driven by a few QPs in the entire device at any given time. In a related work, the dynamics of a population of a few thousands of QPs is probed by $T_1$ measurements of a transmon qubit [26].

The fluxonium qubit [27] [Fig. 1(a)] consists of a Josephson junction shunted by a superinductor [28,29], which is itself an array of large Josephson junctions [30]. An optical image of the fluxonium sample coupled to its readout antenna is shown in Fig. 1(b). An applied external flux $\Phi_{\text{ext}}$ strongly affects the fluxonium spectrum, energy eigenstates, and its susceptibility to different loss mechanisms. The overall quality factor $Q$ of the fluxonium is given by

$$
\frac{1}{Q} = \sum_x \eta_x \frac{p_x}{Q_x},
$$

where $Q_x$ is the quality factor of the material involved in the loss mechanism $x$, $p_x$ is its participation ratio, and $\eta_x$ is the oscillator strength of the qubit transition induced by $x$. Figure 1(c) shows $\eta_x$ as a function of external flux for three main loss mechanisms—capacitive, inductive, and QP tunneling across the small junction. The main inductive loss mechanism for the fluxonium is due to QP tunneling across the array junctions. Note that around $\Phi_{\text{ext}} = \Phi_0/2$, the fluxonium qubit becomes insensitive to loss due to QP...
tunneling across the small junction and maximally sensitive to loss due to QP tunneling across the array junctions.

The insensitivity of the fluxonium qubit to QP tunneling across the small junction was demonstrated by the measurement of a sharp $T_1$ increase to values above 1 ms in the vicinity of $\Phi_0/2$ [20]. In addition, nonexponential decay curves were occasionally measured, suggesting a fluctuating QP population. To gain access to these fluctuations, we improved the readout setup used in Ref. [20] by adding a JPC amplifier, thus increasing the signal-to-noise ratio of the setup by a factor of 10. A schematic of the measurement setup is presented in Fig. 2(a).

To monitor the state of the qubit, we apply a continuous wave drive at the cavity resonance corresponding to an average photon population $\bar{n} = 2.5$. This value is a compromise between fast measurement and the effect of cavity photons which reduce the qubit lifetime and saturate the JPC output [31]. In Fig. 2(b), we show a histogram of measured $I$-$Q$ quadratures at a flux bias point $\Phi_{\text{ext}} = \Phi_0/2$, where the qubit frequency is $\omega_{\text{exc}}/2\pi = 665$ MHz. The measured distributions corresponding to the ground (excited) states of the fluxonium qubit [right (left)] are separated by 5 standard deviations $\sigma$. The relative population of the fluxonium in its excited state (33%) corresponds to an effective temperature of 45 mK.

A few examples of measured qubit quantum jump traces are shown in Fig. 2(c). To estimate the state of the qubit (orange lines) from the time trace of quadrature $I$ (blue lines), we apply a two-point filter. The filter declares a jump in the qubit state if the quadrature value crosses a threshold set $\sigma/2$ away from the jump destination. Otherwise, the qubit is declared to remain in its previous state. The traces suggest there are two regimes with distinctly different jump statistics. There appear to be “quiet” times with few jumps and long intervals between them (on the order of 1 ms) and “noisy” times with many rapid consecutive jumps (less than 100 $\mu$s apart).

Uncorrelated quantum jumps obey Poisson statistics, leading to an exponential distribution of the time spent in the ground or excited state $p_\rho(\tau) = (1/\bar{\tau})e^{-\tau/\bar{\tau}}$, where $\bar{\tau}$ is the mean time spent in the ground or excited state. To enhance the visibility of deviations from Poisson statistics, which would merely show up as a nonexponential decrease of $p(\tau)$, we depict the distribution $\rho(\tau)$ instead. In Figs. 3(a) and 3(b), we show two different second-long measurements of $\rho(\tau)$ distributions for the ground (blue) and excited (red) states, histogrammed with logarithmic bins. The dashed lines correspond to the distribution predicted by Poisson statistics with $\bar{\tau}$ taken as the measured average time either in the ground (blue) or excited (red) state (see the Supplemental Material [31] for a detailed definition). There is significant deviation between the two measurements. In Fig. 3(b), we show a measurement record which we call quiet, apparently agreeing with Poisson statistics. The noisy record in Fig. 3(a) deviates significantly from the Poisson prediction, with long and short times appearing considerably more frequently than expected.

In Fig. 3(c), the mean time spent in the ground (blue) and excited (red) states is shown as a function of time, over several minutes. Each point corresponds to a 1 s temporal average. To quantify the deviation of each measurement from Poisson statistics, we calculate the fidelity of the measured histogram to the Poisson prediction $F = \langle \sum_i \sqrt{M_i P_i / \sum_i M_i} \rangle$, where $M_i$ is the measured ground state histogram value of bin $i$ and $P_i$ is the predicted value of bin $i$ for a Poisson process. In Fig. 3(d), we plot the deviation from Poisson statistics $1 - F$ corresponding to the measurements in Fig. 3(c). These two figures indicate a correlation between long fluxonium energy lifetimes and agreement with Poisson statistics [31]. The noisy seconds appear to have an abundance of short quantum jumps which distort the Poisson statistics, typical for the quiet seconds. Figure 3(e) shows $\bar{\sigma}_z$, the mean polarization of the fluxonium qubit for the same measurements. The fluctuations in polarization are not correlated with the fluctuations between quiet and noisy seconds. The examples in Figs. 3(a) and 3(b) were taken for measurements with
the same polarization corresponding to a temperature of 49 mK [highlighted in gray in Figs. 3(c), 3(d), and 3(e)].

The susceptibility of the fluxonium qubit at $\Phi_{ext} = \Phi_0/2$ to loss due to QPs in the array suggests that fluctuations in the mean time between qubit jumps and their statistics result from the changing QP population. To test this hypothesis, we compare our measurements of spontaneous recombination in the mean time between qubit jumps and their statistics to loss due to QPs in the array suggests that fluctuations in these values over the course of minutes. (d) $1 - F$ (see the text) vs time, quantifying the deviation between the measured histogram and the expected Poisson prediction for the ground state. (e) Average polarization of the fluxonium qubit vs time. The dashed blue line marks the average polarization, which corresponds to a temperature of 46 mK, and the gray dashed line are markers for 40 and 60 mK. Note that the qubit temperature is not correlated with the fluctuations between the quiet and noisy intervals.

Estimate that at least $10^6$ QPs are generated during each pulse. In Figs. 4(a) and 4(b), we show a comparison between measurements of the mean time spent in the ground state without and with QP generation pulses. In the presence of QP generation pulses, the quiet seconds (higher mean time in the ground state) are suppressed [31].

We reduced the number of QPs by cooling down our sample in a constant magnetic field corresponding to $\Phi_0/2$ in the fluxonium loop. Under these conditions, the antenna pads [see Fig. 1(b)] are threaded by flux corresponding to several $\Phi_0$. During the field cooldown process, the pads can trap vortices [32,33], which may act as QP traps due to the reduced superconducting gap in their cores [26,34–36]. Figure 4(c) shows measurements of the mean time spent in the ground state taken after the sample was cooled in
magnetic field. We observe an increase in the number of quiet seconds, indicating a reduction in the number of QPs [31]. The fluxonium effective temperature changes by less than 10 mK between different cooldowns.

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Taking advantage of the real time measurement of the qubit relaxation, we can monitor the time evolution of $\bar{t}$ after a QP generation pulse. In Fig. 4(d), we show the average time spent in the excited state before a jump to the ground state, as a function of time after the QP generation pulse for pulse length $t_G = 50 \mu s$. This yields the equilibration of qubit lifetime as injected QPs leave the junction array. The qubit lifetime eventually saturates to a steady state dominated either by nonthermal QPs or other loss mechanisms. The rate to jump from the excited to the ground state at time $t$ after the pulse is related to the relative QP density by [37]

$$\Gamma_{e-g}(t) = x_{QP}(t) \sqrt{2\Delta \frac{2\pi}{\hbar} \frac{E_L}{\hbar}}. \quad (2)$$

where $x_{QP}$ is the ratio of QPs to Cooper pairs in the junction array and $\Delta$ is the superconducting gap. We fit the lifetime measurements to an exponential model $x_{QP}(t) = x_{QP} + [x_{QP}(0) - x_{QP}] e^{-t/t_{SS}}$ from which we extract the time to reach the QP steady state $t_{SS} = 125 \pm 25 \mu s$ and a non-thermal background QP density $\bar{x}_{QP} = 4 \pm 1 \times 10^{-8}$, corresponding to 1–2 QPs in the whole array. Note that the non-Poissonian jump statistics corresponding to the noisy seconds [see Fig. 3(a)] show fluctuations in the QP number on the order of their average value, also suggesting the presence of only a few QPs in the whole array. This value for $\bar{x}_{QP}$ is an order of magnitude lower than what was measured for the small junction in Ref. [20]. The origin of the difference is presently not understood, although one could speculate that QPs in the array more easily diffuse into the antenna. Note that the value for $\bar{x}_{QP}$ is neither correlated with the QP generation pulse length $t_G$ nor the time to reach the steady state $t_{SS}$ [see the inset of Fig. 4(d)]. The extracted $\bar{x}_{QP}$ should be treated as an upper bound, since contributions from other decay sources could be present. Because of the limited dynamic range of our qubit lifetime measurement, of only a factor of 4, we cannot distinguish between different QP removal mechanisms such as trapping, diffusion, or recombination [31]. The discrimination between these mechanisms was recently demonstrated in a transmon qubit [26].

From the quantum jump traces following a QP generation pulse, we can also extract the average polarization of the qubit and hence its effective temperature. In Fig. 4(e), we show the extracted temperature vs time, starting from 1.4 ms after a QP generation pulse, when the QP population has already saturated. The initial increase in temperature following the QP generation pulse is proportional to the pulse length $t_G$, and it is consistent with an estimated dissipated power of $10^{-10}$ W absorbed in the volume of the sapphire substrate. The temperature equilibration time $t_{eq}$ of several ms is much slower than the sapphire thermalization time and is likely limited by the sapphire-copper contact [31].

In conclusion, the distribution of spontaneous quantum jumps of a fluxonium qubit indicates large relative fluctuations in the energy lifetime of this artificial atom. Corresponding changes of the QP density in the superinductor appear to be the natural explanation. This is supported, in particular, by the increased fluxonium energy lifetime in the presence of QP-trapping vortices, which also render the jump statistics Poissonian. The density of QPs extracted from the measurement does not appear to self-average over periods of seconds, minutes, and even hours. This suggests they originate from sources external to the sample, such as stray infrared [3,38] or higher energy radiation [5,39]. In addition, the fluxonium quantum jump statistics resolves a single QP on a $\mu s$ time scale, which could be a useful property for a low flux, low energy, particle counting detector.
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